

Computation of Some Temperature Indices of $HC_5C_7 [p, q]$ Nanotubes

V.R.Kulli

Department of Mathematics
Gulbarga University, Gulbarga 585 106, India
E-mail: vrkulli@gmail.com

Received 30 October 2019; accepted 25 November 2019

Abstract. In Chemical Science, the connectivity indices are used in the analysis of drug molecular structures which are helpful for chemical scientists, medical scientists and pharmaceutical scientists to find out the chemical and biological characteristics of drugs. In this study, we introduce the first and second hyper temperature indices, sum connectivity temperature index, product connectivity temperature index, reciprocal product connectivity temperature index, general first and second temperature indices, F-temperature index, general temperature index of a molecular graph. Furthermore, we determine these newly defined temperature indices for $HC_5C_7 [p, q]$ nanotubes.

Keywords: Hyper temperature indices, sum connectivity temperature index, product connectivity temperature index, F-temperature index, nanotube.

AMS Mathematics Subject Classification (2010): 05C05, 05C07, 05C12, 05C35

1. Introduction

In this paper, we consider only finite, simple, connected graphs. Let G be such a graph with vertex set $V(G)$ and edge set $E(G)$. The degree $d_G(v)$ of a vertex v is the number of vertices adjacent to v . For undefined concepts and notations, we refer [1].

A molecular graph is a graph whose vertices correspond to the atoms and the edges to the bonds. Studying molecular graphs is a constant focus in Chemical Graph Theory; an effort to better understand molecular structure. Several graph indices have found some applications in Chemistry, especially in QSPR/QSAR study [2, 3, 4].

In [5], Fajtlowicz defined the temperature of a vertex v of a graph G as

$$T(v) = \frac{d_G(v)}{n - d_G(v)},$$

where n is the number of vertices of G .

Motivated by the work on degree based topological indices, we define some temperature indices as follows:

We introduce first and second hyper temperature indices of a graph G , defined as

$$HT_1(G) = \sum_{uv \in E(G)} [T(u) + T(v)]^2, \quad HT_2(G) = \sum_{uv \in E(G)} [T(u)T(v)]^2.$$

V.R.Kulli

We introduce the sum connectivity temperature index of a graph G and it is defined as

$$ST(G) = \sum_{uv \in E(G)} \frac{1}{\sqrt{T(u) + T(v)}}.$$

We propose the product connectivity temperature index of a graph G , defined as

$$PT(G) = \sum_{uv \in E(G)} \frac{1}{\sqrt{T(u)T(v)}}.$$

The reciprocal product connectivity temperature index of a graph G is defined as

$$RPT(G) = \sum_{uv \in E(G)} \sqrt{T(u)T(v)}.$$

The arithmetic-geometric temperature index of a graph G is defined as

$$AGT(G) = \sum_{uv \in E(G)} \frac{T(u) + T(v)}{2\sqrt{T(u)T(v)}}.$$

The general first and second temperature indices of a graph G are defined as

$$T_1^a(G) = \sum_{uv \in E(G)} [T(u) + T(v)]^a, \quad T_2^a(G) = \sum_{uv \in E(G)} [T(u)T(v)]^a,$$

where a is a real number.

We introduce the following temperature indices as follows:

The F -temperature index of a graph G is defined as

$$FT(G) = \sum_{uv \in E(G)} [T(u)^2 + T(v)^2].$$

The general temperature index of a graph G is defined as

$$T_a(G) = \sum_{uv \in E(G)} [T(u)^a + T(v)^a].$$

Recently, some new temperature indices were studied in [6, 7, 8] and also some new connectivity indices were studied, for example, in [9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22,23, 24,25,26,27,28]. In this paper, some newly defined temperature indices of $HC_5C_7[p, q]$ nanotubes are computed.

2. Results for $HC_5C_7[p, q]$ nanotubes

We consider $HC_5C_7[p, q]$ nanotubes in which p is the number of heptagons in the first row and q rows of pentagons repeated alternately. The 2-D lattice of $HC_5C_7[8, 4]$ nanotube is shown in Figure 1.

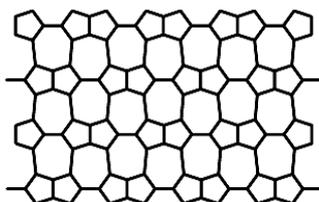


Figure 1: 2-D lattice of $HC_5C_7[8, 4]$ nanotube

Computation of Some Temperature Indices of $HC_5C_7[p, q]$ Nanotubes

Let G be a graph of a nanotube $HC_5C_7[p, q]$. By calculation, G has $4pq$ vertices and $6pq - p$ edges. In G , there are two types of edges based on the temperature of the vertices of each edge as given in Table 1.

$T(u), T(v) \setminus uv \in E(G)$	$\left(\frac{2}{4pq-2}, \frac{3}{4pq-3}\right)$	$\left(\frac{3}{4pq-3}, \frac{3}{4pq-3}\right)$
Number of edges	$4p$	$6pq - 5p$

Table 1: Edge partition of G

Theorem 1. The general first temperature index of a nanotube $HC_5C_7[p, q]$ is

$$T_1^a(HC_5C_7[p, q]) = 4p \left[\frac{20pq - 12}{(4pq - 2)(4pq - 3)} \right]^a + (6pq - 5p) \left(\frac{6}{4pq - 3} \right)^a. \quad (1)$$

Proof: Let $G = HC_5C_7[p, q]$. By definition, we have

$$T_1^a(G) = \sum_{uv \in E(G)} [T(u) + T(v)]^a.$$

Thus by using Table 1, we deduce

$$\begin{aligned} T_1^a(HC_5C_7[p, q]) &= 4p \left(\frac{2}{4pq - 2} + \frac{3}{4pq - 3} \right)^a + (6pq - 5p) \left(\frac{3}{4pq - 3} + \frac{3}{4pq - 3} \right)^a \\ &= 4p \left[\frac{20pq - 12}{(4pq - 2)(4pq - 3)} \right]^a + (6pq - 5p) \left(\frac{6}{4pq - 3} \right)^a. \end{aligned}$$

From Theorem 1, we deduce the following results.

Corollary 1.1. The first hyper temperature index of a nanotube $HC_5C_7[p, q]$ is

$$HT_1(HC_5C_7[p, q]) = 4p \left[\frac{20pq - 12}{(4pq - 2)(4pq - 3)} \right]^2 + (6pq - 5p) \left(\frac{6}{4pq - 3} \right)^2$$

Corollary 1.2. The sum connectivity temperature index of a nanotube $HC_5C_7[p, q]$ is

$$ST(HC_5C_7[p, q]) = 4p \left[\frac{20pq - 12}{(4pq - 2)(4pq - 3)} \right]^{\frac{1}{2}} + (6pq - 5p) \left(\frac{6}{4pq - 3} \right)^{\frac{1}{2}}$$

Proof: Put $a = 2, -\frac{1}{2}$ in equation (1), we obtain the desired results.

Theorem 2. The general second temperature index of a nanotube $HC_5C_7[p, q]$ is

$$T_2^a(HC_5C_7[p, q]) = 4p \left[\frac{6}{(4pq - 2)(4pq - 3)} \right]^a + (6pq - 5p) \left(\frac{3}{4pq - 3} \right)^{2a}. \quad (2)$$

Proof: Let $G = HC_5C_7[p, q]$. By definition, we have

$$T_2^a(G) = \sum_{uv \in E(G)} [T(u)T(v)]^a.$$

Thus by using Table 1, we derive

V.R.Kulli

$$\begin{aligned} T_2^a(HC_5C_7[p, q]) &= 4p \left(\frac{2}{4pq-2} \times \frac{3}{4pq-3} \right)^a + (6pq-5p) \left(\frac{3}{4pq-3} \times \frac{3}{4pq-3} \right)^a \\ &= 4p \left[\frac{6}{(4pq-2)(4pq-3)} \right]^a + (6pq-5p) \left(\frac{3}{4pq-3} \right)^{2a}. \end{aligned}$$

We establish the following results from Theorem 2.

Corollary 2.1. The second hyper temperature index of a nanotube $HC_5C_7[p, q]$ is

$$HT_2(HC_5C_7[p, q]) = 4p \left[\frac{6}{(4pq-2)(4pq-3)} \right]^2 + (6pq-5p) \left(\frac{3}{4pq-3} \right)^4.$$

Corollary 2.2. The product connectivity temperature index of a nanotube $HC_5C_7[p, q]$ is

$$PT(HC_5C_7[p, q]) = \frac{4}{\sqrt{6}} p \sqrt{(4pq-2)(4pq-3)} + \frac{1}{3} (6pq-5p)(4pq-3).$$

Corollary 2.3. The reciprocal product connectivity temperature index of a nanotube $HC_5C_7[p, q]$ is

$$RPT(HC_5C_7[p, q]) = \frac{4\sqrt{6}p}{\sqrt{(4pq-2)(4pq-3)}} + \frac{3(6pq-5p)}{4pq-3}.$$

Proof: Put $a = 2, -\frac{1}{2}, \frac{1}{2}$ in equation (2), we get the desired results.

Theorem 3. The arithmetic-geometric temperature index of a nanotube $HC_5C_7[p, q]$ is given by

$$AGT(HC_5C_7[p, q]) = \frac{2p(20pq-12)}{\sqrt{6(4pq-2)(4pq-3)}} + 6pq-5p.$$

Proof: Let $G = HC_5C_7[p, q]$. By definition, we have

$$AGT(G) = \sum_{uv \in E(G)} \frac{T(u)+T(v)}{2\sqrt{T(u)T(v)}}.$$

Thus by using Table 1, we deduce

$$\begin{aligned} AGT(HC_5C_7[p, q]) &= 4p \left[\left(\frac{2}{4pq-2} + \frac{3}{4pq-3} \right) \div \left(2\sqrt{\frac{2}{4pq-2} \times \frac{3}{4pq-3}} \right) \right] \\ &\quad + (6pq-5p) \left[\left(\frac{3}{4pq-3} + \frac{3}{4pq-3} \right) \div 2\sqrt{\frac{3}{4pq-3} \times \frac{3}{4pq-3}} \right] \\ &= \frac{2p(20pq-12)}{\sqrt{6(4pq-2)(4pq-3)}} + 6pq-5p. \end{aligned}$$

Theorem 4. The general temperature index of a nanotube $HC_5C_7[p, q]$ is given by

Computation of Some Temperature Indices of $HC_5C_7[p, q]$ Nanotubes

$$T_a(HC_5C_7[p, q]) = 4p \left[\left(\frac{2}{4pq-2} \right)^a + \left(\frac{3}{4pq-3} \right)^a \right] + 2(6pq-5p) \left(\frac{3}{4pq-3} \right)^a \quad (3)$$

Proof: Let $G = HC_5C_7[p, q]$. By definition, we have

$$T_a(G) = \sum_{w \in E(G)} [T(u)^a + T(v)^a].$$

Hence by using Table 1, we derive

$$\begin{aligned} T_a(HC_5C_7[p, q]) &= 4p \left[\left(\frac{2}{4pq-2} \right)^a + \left(\frac{3}{4pq-3} \right)^a \right] \\ &\quad + (6pq-5p) \left[\left(\frac{3}{4pq-3} \right)^a + \left(\frac{3}{4pq-3} \right)^a \right] \\ &= 4p \left[\left(\frac{2}{4pq-2} \right)^a + \left(\frac{3}{4pq-3} \right)^a \right] + 2(6pq-5p) \left(\frac{3}{4pq-3} \right)^a. \end{aligned}$$

We obtain the following result from Theorem 4.

Corollary 4.1. The F-temperature index of a nanotube $HC_5C_7[p, q]$ is

$$FT(HC_5C_7[p, q]) = pq \frac{108}{(4pq-3)^2} + p \left[\frac{16}{(4pq-2)^2} - \frac{54}{(4pq-3)^2} \right].$$

Proof: Put $a = 2$ in equation (3), we get the desired result.

5. Conclusion

In this study, the expressions for the first and second hyper temperature indices, sum connectivity temperature index, product connectivity temperature index, arithmetic-geometric temperature index, F -temperature index, general first and second temperature indices of $HC_5C_7[p, q]$ nanotubes have been computed.

Acknowledgement. The author is thankful to the referee for his/her suggestions.

REFERENCES

1. V.R.Kulli, *Collegiate Graph Theory*, Vishwa International Publications, Gulbarga, India (2012).
2. I.Gutman and O.E.Polansky, *Mathematical Concepts in Organic Chemistry*, Springer, Berlin (1986).
3. V.R.Kulli, *Multiplicative Connectivity Indices of Nanostructures*, LAP LEMBERT Academic Publishing, (2018).
4. R.Todeschini and V.Consonni, *Handbook of Molecular Descriptors for Chemoinformatics*, Wiley-VCH, Weinheim, (2000).
5. S.Fajtlowicz, On conjectures of Graffitti, *Discrete Math.*, 72(1988) 113-118.
6. V.R.Kulli, Some new temperature indices of oxide and honeycomb networks, submitted.
7. V.R.Kulli, Some multiplicative temperature indices of $HC_5C_7[p, q]$ nanotubes, *International Journal of Fuzzy Mathematical Archive*, to appear.

V.R.Kulli

8. V.R.Kulli, Computing some new multiplicative temperature indices of certain networks, submitted.
9. B.Zhou, Zagreb indices, *MATCH Commun.Math. Comput. Chem.*, 52 (2004) 113-118.
10. V.R.Kulli, On the sum connectivity reverse index of oxide and honeycomb networks, *Journal of Computer and Mathematical Sciences*, 8(9) (2017) 408-413.
11. V.R.Kulli, On the product connectivity reverse index of silicate and hexagonal networks, *International Journal of Mathematics and its Applications*, 5(4-B) (2017) 175-179.
12. V.R.Kulli, The sum connectivity Revan index of silicate and hexagonal networks, *Annals of Pure and Applied Mathematics*, 14(3) (2017) 401-406.
13. V.R.Kulli, Multiplicative connectivity indices of certain nanotubes, *Annals of Pure and Applied Mathematics*, 12(2) (2016) 169-176.
14. V.R.Kulli, Multiplicative connectivity Revan indices of polycyclic aromatic hydrocarbons and benzenoid systems, *Annals of Pure and Applied Mathematics*, 16(2) (2018) 336-343.
15. V.R.Kulli, Two new arithmetic-geometric ve-degree indices, *Annals of Pure and Applied Mathematics*, 17(1) (2018) 107-112.
16. V.R.Kulli, Product connectivity leap index and ABC leap index of helm graphs, *Annals of Pure and Applied Mathematics*, 18(2) (2018) 189-193.
17. V.R.Kulli, Computing reduced connectivity indices of certain nanotubes, *Journal of Chemistry and Chemical Sciences*, 8(11) (2018) 1174-1180.
18. V.R.Kulli, On connectivity KV indices of certain families of dendrimers, *International Journal of Mathematical Archive*, 10(2) (2019) 14-17.
19. V.R.Kulli, New connectivity topological indices, *Annals of Pure and Applied Mathematics*, 20(1) (2019) 1-8.
20. V.R.Kulli, Multiplicative ABC, GA and AG neighborhood Dakshayani indices of dendrimers, *International Journal of Fuzzy Mathematical Archive*, 17(2) (2019) 77-82.
21. V.R.Kulli, Some new multiplicative connectivity Kulli-Basava indices, *International Journal of Mathematics Trends and Technology*, 65(9) (2019) 18-23.
22. V.R.Kulli, Connectivity neighborhood Dakshayani indices of POPAM dendrimers, *Annals of Pure and Applied Mathematics*, 20(1) (2019) 49-54.
23. V.R.Kulli, Some new status indices of graphs, *International Journal of Mathematics Trends and Technology*, 65(10) (2019) 70-76.
24. V.R.Kulli, Some new multiplicative status indices of graphs, *International Journal of Recent Scientific Research*, 10(10) (2019) 35568-35573.
25. V.R.Kulli, B.Chaluvaraju, H.S.Boregowda, The Product connectivity Banhatti index of a graph, *Discussiones Mathematicae, Graph Theory*, (2019) doi: 10.7151/dmgt.2098
26. M.Randić, On characterization of molecular branching, *J. Am. Chem. Soc.*, 97 (1975) 6609-6615.
27. B.Zhou and N.Trinajstić, On a novel connectivity index, *J. Math. Chem.*, 46 (2009) 1252-1270.
28. B.Zhou and N.Trinajstić, On general sum connectivity index, *J. Math. Chem.*, 47 (2010) 210-218.