Intern. J. Fuzzy Mathematical Archive Vol. 12, No. 1, 2017, 29-37 ISSN: 2320–3242 (P), 2320–3250 (online) Published on 27 March 2017 www.researchmathsci.org DOI: http://dx.doi.org/10.22457/ijfma.v12n1a4

International Journal of **Fuzzy Mathematical Archive** 

# New K-Banhatti Topological Indices

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Received 20 March 2017; accepted 26 March 2017

*Abstract.* In this paper, we introduce the modified first and second *K* Banhatti indices of a graph. Also we introduce the harmonic *K*-Banhatti index of a graph. We initiate a study of these new invariants.

*Keywords:* modified first and second *K*-Banhatti indices, harmonic *K*-Banhatti index, nanotubes

# AMS Mathematics Subject Classification (2010): 05C05, 05C07, 05C35

#### 1. Introduction

Let *G* be a finite, simple connected graph. The degree  $d_G(v)$  of a vertex *v* is the number of vertices adjacent to *v*. The edge connecting vertices *u* and *v* is denoted by *uv*. If e = uv is an edge of *G*, then the vertex *u* and edge *e* are incident as are *v* and e. Let  $d_G(e)$  denote the degree of an edge *e* in *G*, which is defined by  $d_G(e) = d_G(u) + d_G(v) - 2$  with e = uv. Any undefined term here may be found in Kulli [1].

A molecular graph is a graph such that its vertices correspond to the atoms and the edges to the bonds. Chemical graph theory is a branch of Mathematical chemistry which has an important effect on the development of the chemical sciences. A single number that can be used to characterize some property of the graph of a molecular is called a topological index for that graph. Numerous topological descriptors have found some applications in theoretical chemistry especially in QSPR/QSAR research.

The modified first and second Zagreb indices [2] are respectively defined as

$${}^{m}M_{1}(G) = \sum_{u \in V(G)} \frac{1}{d_{G}(u)^{2}}, \qquad {}^{m}M_{2}(G) = \sum_{u v \in E(G)} \frac{1}{d_{G}(u)d_{G}(v)}.$$

These indices were studied by Kulli in [3, 4].

Motivated by the definition of the modified first and second Zagreb indices, we introduce the modified first and second *K*-Banhatti indices of a graph as follows:

The modified first and second K-Banhatti indices of a graph are defined as

$${}^{m}B_{1}(G) = \sum_{ue} \frac{1}{d_{G}(u) + d_{G}(e)}, {}^{m}B_{2}(G) = \sum_{ue} \frac{1}{d_{G}(u)d_{G}(e)}.$$

where ue means that the vertex u and edge e are incident in G.

The harmonic index of a graph G is defined as

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$$H(G) = \sum_{uv \in E(G)} \frac{2}{d_G(u) + d_G(v)}.$$

This index was studied by Favaron et.al. [5] and Zhong [6].

Motivated by the definition of the harmonic index and by previous research on topological indices, we now introduce the harmonic K-Banhatti index of a graph as follows:

The harmonic K-Banhatti index of a graph G is defined as

$$H_b(G) = \sum_{ue} \frac{2}{d_G(u) + d_G(e)}$$

where ue means that the vertex u and edge e are incident in G.

Many other topological indices were studied, for example, in [7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18].

In this paper, we compute the modified first and second K Banhatti indices and harmonic K Banhatti index of some standard graphs,  $TUC_4C_8[p, q]$  nanotubes and  $TUC_4[p, q]$  nanotubes.

# 2. Computing K Banhatti topological indices of some standard graphs

**Theorem 1.** Let  $C_n$  be a cycle with  $n \ge 3$  vertices. Then

(1) 
$${}^{m}B_{1}(C_{n}) = \frac{1}{2}n$$
 (2)  ${}^{m}B_{2}(C_{n}) = \frac{1}{2}n$  (3)  $H_{b}(C_{n}) = n$ 

**Proof:** Let  $G = C_n$  be a cycle with  $n \ge 3$  vertices. Every vertex of a cycle  $C_n$  is incident with exactly two edges and the number of edges in  $C_n$  is n.

$$(1) \qquad {}^{m}B_{1}(G) = \sum_{ue} \frac{1}{d_{G}(u) + d_{G}(e)} = \sum_{uv \in E(G)} \left( \frac{1}{d_{G}(u) + d_{G}(e)} + \frac{1}{d_{G}(v) + d_{G}(e)} \right)$$
$$= \left( \frac{1}{2+2} + \frac{1}{2+2} \right) n = \frac{1}{2} n.$$
$$(2) \qquad {}^{m}B_{2}(G) = \sum_{ue} \frac{1}{d_{G}(u)d_{G}(e)} = \sum_{uv \in E(G)} \left( \frac{1}{d_{G}(u)d_{G}(e)} + \frac{1}{d_{G}(v)d_{G}(e)} \right)$$
$$= \left( \frac{1}{2\times2} + \frac{1}{2\times2} \right) n = \frac{1}{2} n.$$
$$(3) \qquad H_{b}(G) = \sum_{ue} \frac{2}{d_{G}(u) + d_{G}(e)} = 2\sum_{ue} \frac{1}{d_{G}(u) + d_{G}(e)} = n.$$

**Theorem 2.** Let  $P_n$  be a path with  $n \ge 3$  vertices. Then

(1) 
$${}^{m}B_{1}(P_{n}) = \frac{1}{2}n + \frac{1}{6}$$
 (2)  ${}^{m}B_{2}(P_{n}) = \frac{1}{2}n + \frac{3}{2}$  (3)  $H_{b}(P_{n}) = n + \frac{1}{3}$ .

**Proof:** Let  $G = P_n$  be a path with  $n \ge 3$  vertices. We obtain two partitions of the edge set of  $P_n$  as follows:

 $E_3 = \{e = uv \in E(G) \mid d_G(u) = 1, \, d_G(v) = 2\}, \, |E_3| = 2.$ 

 $E_{4} = \{e = uv \in E(G) \mid d_{G}(u) = d_{G}(v) = 2\}, |E_{4}| = n - 3.$ (1) To compute  ${}^{m}B_{1}(P_{n})$ , we see that  ${}^{m}B_{1}(G) = \sum_{ue} \frac{1}{d_{G}(u) + d_{G}(e)} = \sum_{uv \in E_{3}} \left(\frac{1}{d_{G}(u) + d_{G}(e)} + \frac{1}{d_{G}(v) + d_{G}(e)}\right)$   $+ \sum_{uv \in E_{4}} \left(\frac{1}{d_{G}(u) + d_{G}(e)} + \frac{1}{d_{G}(v) + d_{G}(e)}\right)$   $= \left(\frac{1}{1+1} + \frac{1}{2+1}\right) 2 + \left(\frac{1}{2+2} + \frac{1}{2+2}\right) (n-3) = \frac{1}{2}n + \frac{1}{6}.$ (2) To compute  ${}^{m}B_{1}(P_{1})$ , we see that

(2) To compute  ${}^{m}B_{2}(P_{n})$ , we see that

$${}^{m}B_{2}(G) = \sum_{ue} \frac{1}{d_{G}(u)d_{G}(e)}$$
$$= \sum_{uv \in E_{3}} \left(\frac{1}{d_{G}(u)d_{G}(e)} + \frac{1}{d_{G}(v)d_{G}(e)}\right) + \sum_{uv \in E_{4}} \left(\frac{1}{d_{G}(u)d_{G}(e)} + \frac{1}{d_{G}(v)d_{G}(e)}\right)$$
$$= \left(\frac{1}{1 \times 1} + \frac{1}{2 \times 1}\right) 2 + \left(\frac{1}{2 \times 2} + \frac{1}{2 \times 2}\right) (n-3) = \frac{1}{2}n + \frac{3}{2}.$$

(3) To compute  $H_b(P_n)$ , we see that

$$H_{b}(G) = \sum_{ue} \frac{2}{d_{G}(u) + d_{G}(e)} = 2\sum_{ue} \frac{1}{d_{G}(u) + d_{G}(e)} = n + \frac{1}{3}$$

**Theorem 3.** Let  $K_n$  be a complete graph with  $n \ge 3$  vertices. Then

(1) 
$${}^{m}B_{1}(K_{n}) = \frac{n(n-1)}{3n-5}$$
 (2)  ${}^{m}B_{2}(K_{n}) = \frac{n}{2(n-2)}$  (3)  $H_{b}(K_{n}) = \frac{2n(n-1)}{3n-5}$ 

Proof: Let  $G = K_n$  be a complete graph with  $n \ge 3$  vertices. Every vertex of  $K_n$  is incident with exactly n - 1 edges.

(1) To compute  ${}^{m}B_{1}(K_{n})$ , we see that

$${}^{m}B_{1}(G) = \sum_{ue} \frac{1}{d_{G}(u) + d_{G}(e)} = \sum_{uv \in E(G)} \left(\frac{1}{d_{G}(u) + d_{G}(e)} + \frac{1}{d_{G}(v) + d_{G}(e)}\right)$$
$$= \left(\frac{1}{(n-1) + (2n-4)} + \frac{1}{(n-1) + (2n-4)}\right) \frac{n(n-1)}{2} = \frac{n(n-1)}{3n-5}.$$

(2) To compute  ${}^{m}B_{2}(K_{n})$ , we see that

$${}^{m}B_{2}(G) = \sum_{ue} \frac{1}{d_{G}(u)d_{G}(e)} = \sum_{uv \in E(G)} \left(\frac{1}{d_{G}(u)d_{G}(e)} + \frac{1}{d_{G}(v)d_{G}(e)}\right)$$
$$= \left(\frac{1}{(n-1)(2n-4)} + \frac{1}{(n-1)(2n-4)}\right) \frac{n(n-1)}{2} = \frac{n}{2(n-2)}$$
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(3) To compute  $H_b(K_n)$ , we see that

$$H_b(G) = \sum_{ue} \frac{2}{d_G(u) + d_G(e)} = 2\sum_{ue} \frac{1}{d_G(u) + d_G(e)} = \frac{2n(n-1)}{3n-5}.$$

**Theorem 4.** Let  $K_{r,s}$  be a complete bipartite graph with  $1 \le r \le s$  and  $s \ge 2$ . Then

(1) 
$${}^{m}B_{1}(K_{r,s}) = \left(\frac{1}{r+2s-2} + \frac{1}{2r+s-2}\right)rs$$
 (2)  ${}^{m}B_{2}(K_{r,s}) = \frac{r+s}{r+s-2}$   
(3)  $H_{b}(K_{r,s}) = \left(\frac{1}{r+2s-2} + \frac{1}{2r+s-2}\right)2rs.$ 

**Proof:** Let  $G = K_{r,s}$  be a complete bipartite graph with r + s vertices and rs edges such that  $|V_1| = r \ge 1$ ,  $|V_2| = s \ge 2$   $r \le s$ ,  $V(K_{r,s}) = V_1 U V_2$ . Every vertex of  $V_1$  is incident with s edges and every vertex of  $V_2$  is incident with r edges.

(1) To compute  ${}^{m}B_{1}(K_{r,s})$ , we see that

$${}^{m}B_{1}(G) = \sum_{ue} \frac{1}{d_{G}(u) + d_{G}(e)} = \sum_{uv \in E(G)} \left( \frac{1}{d_{G}(u) + d_{G}(e)} + \frac{1}{d_{G}(v) + d_{G}(e)} \right)$$
$$= \left( \frac{1}{s + (r + s - 2)} + \frac{1}{r + (r + s - 2)} \right) rs = \left( \frac{1}{r + 2s - 2} + \frac{1}{2r + s - 2} \right) rs.$$

(2) To compute  ${}^{m}B_{1}(K_{r,s})$ , we see that

$${}^{m}B_{2}(G) = \sum_{ue} \frac{1}{d_{G}(u)d_{G}(e)} = \sum_{uv \in E(G)} \left(\frac{1}{d_{G}(u)d_{G}(e)} + \frac{1}{d_{G}(v)d_{G}(e)}\right)$$
$$= \left(\frac{1}{s(r+s-2)} + \frac{1}{r(r+s-2)}\right)rs = \frac{r+s}{r+s-2}.$$

(3) To compute  $H_b(K_{r,s})$ , we see that

$$H_b(G) = \sum_{ue} \frac{2}{d_G(u) + d_G(e)} = 2\sum_{ue} \frac{1}{d_G(u) + d_G(e)} = \left(\frac{1}{r + 2s - 2} + \frac{1}{2r + s - 2}\right) 2rs$$

**Corollary 1.** Let  $K_{r,s}$  be a complete bipartite graph with  $1 \le r \le s$  and  $s \ge 2$ . Then

(1) 
$${}^{m}B_{1}(K_{r,s}) = \frac{2r^{2}}{3r-2}, \quad \text{if } s = r,$$
  
 $= \frac{3s-1}{2s-1}, \quad \text{if } r = 1.$ 

(2) 
$${}^{m}B_{2}(K_{r,s}) = \frac{r}{r-1}, \quad \text{if } s = r,$$
  
 $= \frac{s+1}{r}, \quad \text{if } r = 1.$ 

$$=\frac{1}{s-1}, \qquad \text{if } r=1$$

(3) 
$$H_b(K_{r,s}) = \frac{4r^2}{3r-2}, \quad \text{if } s = r,$$

$$=\frac{2(3s-1)}{2s-1}$$
, if  $r=1$ .

**Theorem 5.** Let *G* be an *r*-regular graph with  $n \ge 3$  vertices. Then

(1) 
$${}^{m}B_{1}(G) = \frac{nr}{3r-2}$$
 (2)  ${}^{m}B_{2}(G) = \frac{n}{2(r-1)}$  (3)  $H_{b}(G) = \frac{2nr}{3r-2}$ .

**Proof:** Let *G* be an *r*-regular graph with  $n \ge 3$  vertices and  $\frac{nr}{2}$  edges. Every vertex of *G* is incident with *r* edges.

(1) To compute  ${}^{m}B_{1}(G)$ , we see that

$${}^{m}B_{1}(G) = \sum_{ue} \frac{1}{d_{G}(u) + d_{G}(e)} = \sum_{uv \in E(G)} \left( \frac{1}{d_{G}(u) + d_{G}(e)} + \frac{1}{d_{G}(v) + d_{G}(e)} \right)$$
$$= \left( \frac{1}{r + (2r - 2)} + \frac{1}{r + (2r - 2)} \right) \frac{nr}{2} = \frac{nr}{3r - 2}.$$

(2) To compute  ${}^{m}B_{2}(G)$ , we see that

$${}^{m}B_{2}(G) = \sum_{ue} \frac{1}{d_{G}(u)d_{G}(e)} = \sum_{uv \in E(G)} \left(\frac{1}{d_{G}(u)d_{G}(e)} + \frac{1}{d_{G}(v)d_{G}(e)}\right)$$
$$= \left(\frac{1}{r(2r-2)} + \frac{1}{r(2r-2)}\right) \frac{nr}{2} = \frac{n}{2(r-1)}.$$

(3) To compute  $H_b(G)$ , we see that

$$H_{b}(G) = \sum_{ue} \frac{2}{d_{G}(u) + d_{G}(e)} = 2\sum_{ue} \frac{1}{d_{G}(u) + d_{G}(e)} = \frac{2nr}{3r-2}.$$

# 3. Computing K Banhatti type indices of $TUC_4C_8[p, q]$ nanotubes

We discuss  $TUC_4C_8[S]$  nanotubes which are consisting of cycles  $C_4$  and  $C_8$ . These nanotubes usually symbolized as  $TUC_4C_8[p, q]$  for  $p, q \in N$  in which p is the number of octagons  $C_8$  in the first row and q is the number of octagons  $C_8$  in the first column. The 2-dimensional lattice of  $TUC_4C_8[p, q]$  is shown in Figure 1.



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We determine the modified first K Banhatti index of  $TUC_4C_8[p, q]$  nanotubes.

**Theorem 6.** Let  $G = TUC_4C_8[p, q]$  be the graph of nanotubes. Then

$$^{m}B_{1}(G) = \frac{24}{7}pq + \frac{199}{105}p.$$

**Proof:** Let  $G = TUC_4C_8[p, q]$ . By algebraic method, we get |V(G)| = 8pq + 4p and |E(G)| = 12pq + 4p. From Figure 1, it is easy to see that there are three partitions of the edge set of *G* as follows:

$$E_4 = \{e = uv \in E(G) \mid d_G(u) = d_G(v) = 2\}, |E_4| = 2p.$$
  

$$E_5 = \{e = uv \in E(G) \mid d_G(u) = 2, d_G(v) = 3\}, |E_5| = 4p.$$
  

$$E_6 = \{e = uv \in E(G) \mid d_G(u) = d_G(v) = 3\}, |E_6| = 12pq - 2p.$$

Further the edge degree partition of the nanotube  $TUC_4C_8[p, q]$  is given in Table 1.

$d_G(u), d_G(v) \setminus e = uv \in E(G)$	(2, 2)	(2, 3)	(3,3)
$d_G(e)$	2	3	4
Number of edges	2p	4 <i>p</i>	12pq - 2p

**Table 1:** Edge degree partition of  $TUC_4C_8[p, q]$ 

To determine  ${}^{m}B_{1}(G)$ , we see that

$${}^{m}B_{1}(G) = \sum_{ue} \frac{1}{d_{G}(u) + d_{G}(e)} = \sum_{uv \in E_{4}} \left( \frac{1}{d_{G}(u) + d_{G}(e)} + \frac{1}{d_{G}(v) + d_{G}(e)} \right)$$

$$+ \sum_{uv \in E_{5}} \left( \frac{1}{d_{G}(u) + d_{G}(e)} + \frac{1}{d_{G}(v) + d_{G}(e)} \right) + \sum_{uv \in E_{6}} \left( \frac{1}{d_{G}(u) + d_{G}(e)} + \frac{1}{d_{G}(v) + d_{G}(e)} \right)$$

$$= \left( \frac{1}{2 + 2} + \frac{1}{2 + 2} \right) 2p + \left( \frac{1}{2 + 3} + \frac{1}{3 + 3} \right) 4p + \left( \frac{1}{3 + 4} + \frac{1}{3 + 4} \right) (12pq - 2p)$$

$$= \frac{24}{7}pq + \frac{199}{105}p.$$

We determine the modified second K Banahatti index of  $TUC_4C_8[p, q]$  nanotube.

**Theorem 7.** Let  $G = TUC_4C_8[p, q]$  be the graph of nanotubes. Then

$$^{m}B_{2}(G) = 2pq + \frac{16}{9}p.$$

**Proof:** Let  $G = TUC_4C_8[p, q]$  the nanotubes. By using the results from the proof of Theorem 6, we obtain

$${}^{m}B_{2}(G) = \sum_{ue} \frac{1}{d_{G}(u)d_{G}(e)} = \sum_{uv \in E_{4}} \left( \frac{1}{d_{G}(u)d_{G}(e)} + \frac{1}{d_{G}(v)d_{G}(e)} \right)$$

$$+ \sum_{uv \in E_{s}} \left( \frac{1}{d_{G}(u)d_{G}(e)} + \frac{1}{d_{G}(v)d_{G}(e)} \right) + \sum_{uv \in E_{s}} \left( \frac{1}{d_{G}(u)d_{G}(e)} + \frac{1}{d_{G}(v)d_{G}(e)} \right)$$

$$= \left( \frac{1}{2 \times 2} + \frac{1}{2 \times 2} \right) 2p + \left( \frac{1}{2 \times 3} + \frac{1}{3 \times 3} \right) 4p + \left( \frac{1}{3 \times 4} + \frac{1}{3 \times 4} \right) (12pq - 2p)$$

$$= 2pq + \frac{16}{9}p.$$

We compute the harmonic K-Banhatti index of  $TUC_4C_8[p, q]$  nanotube.

**Theorem 8.** Let  $G = TUC_4C_8[p, q]$  be the graph of nanotubes. Then

$$H_b(G) = \frac{48}{7}pq + \frac{398}{105}p.$$

**Proof:** Let  $G = TUC_4C_8[p, q]$  be the nanotubes. By using Theorem 6, we obtain

$$H_b(G) = \sum_{ue} \frac{2}{d_G(u) + d_G(e)} = 2\sum_{ue} \frac{1}{d_G(u) + d_G(e)} = \frac{48}{7}pq + \frac{298}{105}p$$

# 4. Computing *K* Banhatti type indices of $TUC_4[p, q]$ nanotubes.

In this section, we focus on the structures of a family of nanostructures and they are called  $TUHRC_4[S]$  nanotubes. These nanotubes usually symbolized as  $TUC_4[p, q]$  for any  $p, q \in N$  in which p is the number of cycles  $C_4$  in the first row and q is the number of cycles  $C_4$  is the first column as depicted in Figure 2.



**Figure 2:** 2-*D* graph of *G* = *TUC*<sub>4</sub>[*p*, *q*]

We compute the modified first K-Banhatti index of  $TUC_4[p, q]$  nanotubes.

**Theorem 9.** Let *G* be the  $TUC_4[p, q]$  nanotubes. Then

$$^{m}B_{1}(G) = \frac{4}{5}pq + \frac{23}{30}p.$$

**Proof:** Let *G* be the  $TUC_4[p, q]$  nanotubes as depicted in Figure 2. By algebraic method, we obtain |E(G)| = 4pq + 2p. From Figure 2, it is easy to see that there are two partitions of the edge set of *G* as follows:

 $E_6 = \{e = uv \in E(G) \mid d_G(u) = 2, d_G(v) = 4\}, |E_6| = 4p.$   $E_8 = \{e = uv \in E(G) \mid d_G(u) = d_G(v) = 4\}, |E_8| = 4pq - 2p.$ Further the edge degree partition of the nanotube  $TUC_4[p, q]$  is given in Table 2.

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$d_G(u) \ d_G(v) \backslash e = uv \in E(G)$	(2, 4)	(4, 4)
$d_G(e)$	4	6
Number of edges	4p	4pq - 2p

**Table 2:** Edge degree partition of  $TUC_4[p, q]$ 

To compute  ${}^{m}B_{1}(G)$ , we see that

$${}^{m}B_{1}(G) = \sum_{ue} \frac{1}{d_{G}(u) + d_{G}(e)}$$
  
=  $\sum_{uv \in E_{6}} \left(\frac{1}{d_{G}(u) + d_{G}(e)} + \frac{1}{d_{G}(v) + d_{G}(e)}\right) + \sum_{uv \in E_{8}} \left(\frac{1}{d_{G}(u) + d_{G}(e)} + \frac{1}{d_{G}(v) + d_{G}(e)}\right)$   
=  $\left(\frac{1}{2+4} + \frac{1}{4+4}\right) 4p + \left(\frac{1}{4+6} + \frac{1}{4+6}\right) (4pq - 2p) = \frac{4}{5}pq + \frac{23}{30}p.$ 

We compute the modified second K-Banhatti index of  $TUC_4[p, q]$  nanotubes.

**Theorem 10.** Let  $G = TUC_4[p, q]$  be the nanotubes. Then

 $^{m}B_{2}(G) = \frac{1}{3}pq + \frac{7}{12}p.$ 

**Proof:** Let  $G = TUC_4[p, q]$  be the nanotubes. By using the results from the proof of Theorem 9, we obtain

$${}^{m}B_{2}(G) = \sum_{ue} \frac{1}{d_{G}(u)d_{G}(e)}$$
  
=  $\sum_{uv \in E_{6}} \left(\frac{1}{d_{G}(u)d_{G}(e)} + \frac{1}{d_{G}(v)d_{G}(e)}\right) + \sum_{uv \in E_{8}} \left(\frac{1}{d_{G}(u)d_{G}(e)} + \frac{1}{d_{G}(v)d_{G}(e)}\right)$   
=  $\left(\frac{1}{2 \times 4} + \frac{1}{4 \times 4}\right) 4p + \left(\frac{1}{4 \times 6} + \frac{1}{4 \times 6}\right) (4pq - 2p) = \frac{1}{3}pq + \frac{7}{12}p.$ 

We now compute the harmonic K-Banhatti index of  $TUC_4[p,q]$  nanotubes.

**Theorem 11.** Let  $G = TUC_4[p, q]$  be the nanotubes. Then

$$H_b(G) = \frac{8}{5}pq + \frac{23}{15}p.$$

**Proof:** Let  $G = TUC_4[p, q]$  be the nanotubes. By using Theorem 9, we obtain

$$H_b(G) = \sum_{ue} \frac{2}{d_G(u) + d_G(e)} = 2\sum_{ue} \frac{1}{d_G(u) + d_G(e)} = \frac{8}{5}pq + \frac{23}{15}p.$$

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