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# Equitable Regular Total Semi-µ Strong (Weak) Edge Domination in Intuitionistic Fuzzy Graph

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Abstract. In this paper, the new kind of parameter Regular total semi -  $\mu$  strong (weak) edge domination number in an intuitionistic fuzzy graph is defined and established the parametric conditions. Another new kind of parameter an equitable regular total semi -  $\mu$  strong (weak) edge domination number is defined and established the parametric conditions. The properties of Regular total semi -  $\mu$  strong (weak) edge domination number and an equitable regular total semi -  $\mu$  strong (weak) edge domination number and an equitable regular total semi -  $\mu$  strong (weak) edge domination number and an equitable regular total semi -  $\mu$  strong (weak) edge domination number are discussed.

*Keywords:* Dominating set, total semi -  $\mu$  strong (weak) edge domination set, Regular total semi -  $\mu$  strong (weak) edge domination set, equitable regular total semi -  $\mu$  strong (weak) edge domination set, equitable regular total semi -  $\mu$  strong (weak) edge domination number.

AMS Mathematics Subject Classification (2010): 03E72, 05C69, 05C72, 05C76

#### **1. Introduction**

In the year 2003, Nagoor Gani and Basheer Ahamed [8] investigated Order and Size in fuzzy graph. In 2010, Nagoor Gani and Begum[10] investigated Degree, Order and Size of an Intuitionistic Fuzzy Graph. In the year 2016, Karunambigai and Bhuvaneswari [7], investigated Degree in Intuitionistic fuzzy graph. In 2010, Parvathi and Tamizhendhi [11] introduced Domination in intuitionistic fuzzy graph. In the year 2014, Dharmalingam and Rani [2,3], investigated the concepts of Equitable Domination in Fuzzy graphs. In the year 1991, Kulli and Patwari [6] investigated the concepts of on the total edge domination number of a graph In the year 2008, NagoorGani and Prasannadevi [9] proposed Edge domination and independence in fuzzy graph. In 2012, Jayalakshmi et al. [4] introduced total strong (weak) domination in fuzzy graph. In 2016, Jayalakshmi et al. [5] introduced total semi -  $\mu$  strong (weak) domination in intuitionistic fuzzy graph. In this paper, we introduced Equitable Regular Total semi -  $\mu$  strong (weak) domination in

intuitionistic fuzzy graph and some parametric conditions are established as a new concept.

#### 2. Preliminaries

In this section, some basic definitions are discussed.

**Definition 2.1.** [7] Let G = (V, E) be an intuitionistic fuzzy graph (IFG) where  $V = \{v_1, v_2, ..., v_n\}$ . Then,

- i.  $\mu_1 : V \to [0, 1]$  and  $\gamma_1 : V \to [0, 1]$  respectively denote the degree of membership and non-membership of the element  $v_i \in V$  and  $0 \le \mu_1(v_i) + \gamma_1(v_i) \le 1$  for every  $v_i \in V$ .
- ii.  $E \subset V \times V$  where  $\mu_2: V \times V \to [0,1]$  and  $\gamma_2: V \times V \to [0,1]$  are such that  $\mu_2(v_i, v_j) \le \min\{\mu_1(v_i), \mu_1(v_j)\}, \ \gamma_2(v_i, v_j) \le \max\{\gamma_1(v_i), \gamma_1(v_j)\}$  and  $0 \le \mu_2(v_i, v_j) + \gamma_2(v_i, v_j) \le 1$  for every  $(v_i, v_j) \in E$ .

**Definition 2.2.[10]** Let G = (V, E) be an IFG. Then the **cardinality of G** is defined to be  $|G| = \left| \sum_{V_i \in V} \left[ \frac{(1 + \mu_1(v_i) - \gamma_1(v_i))}{2} \right] + \sum_{V_i \in V} \left[ \frac{(1 + \mu_2(v_i, v_j) - \gamma_2(v_i, v_j))}{2} \right] \right|$ 

Definition 2.3. [10] The fuzzy vertex cardinality of G is defined by

$$\mathbf{p} = |\mathbf{V}| = \left| \sum_{\mathbf{v}_i \in \mathbf{V}} \left| \frac{(1 + \mu_1(\mathbf{v}_i) - \gamma_1(\mathbf{v}_i))}{2} \right| \text{ for all } \mathbf{v}_i \in V$$

**Definition 2.4.** [10] The fuzzy edge cardinality of G is defined by  $\begin{bmatrix} 1 \\ 1 \end{bmatrix}$ 

$$\mathbf{q} = |\mathbf{E}| = \left| \sum_{\mathbf{v}_i \in \mathbf{V}} \left[ \frac{(1 + \mu_2(\mathbf{v}_i, \mathbf{v}_j) - \gamma_2(\mathbf{v}_i, \mathbf{v}_j))}{2} \right] \right| \text{ for all } (v_i, v_j) \in \mathbf{E}.$$

Definition 2.5. [8]

Let G =  $\langle V, E \rangle$  be an IFG. Then the **order** of G is defined to be O(G) =  $(O_{\mu}(G), O_{\gamma}(G))$  where  $O_{\mu}(G) = \sum_{\nu_i \in V} \mu_1(\nu_i)$  and  $O_{\gamma}(G) = \sum_{\nu_i \in V} \gamma_1(\nu_i)$ **Definition 2.6. [8]** The **Size** of G is defined to be S(G) =  $(S_{\mu}(G), S_{\gamma}(G))$  where  $S_{\mu}(G)$ 

$$= \sum_{i \neq j} \mu_2(v_i, v_j) \text{ and } S_{\gamma}(G) = \sum_{i \neq j} \gamma_2(v_i, v_j)$$

**Definition 2.7. [8]** Let G =  $((\mu_1, \gamma_1), (\mu_2, \gamma_2))$  be an IFG. The  $\mu$ -degree of a vertex v<sub>i</sub> is  $d_{\mu}(v_i) = \sum_{(v_i, v_j) \in E} \mu_2(v_i, v_j)$ . The  $\gamma$ -degree of a vertex v<sub>i</sub> is  $d_{\gamma}(v_i) = \sum_{(v_i, v_j) \in E} \gamma_2(v_i, v_j)$ .

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The **degree of a vertex** is  $d(v_i) = \left[\sum_{(v_i, v_j) \in E} \mu_2(v_i, v_j), \sum_{(v_i, v_j) \in E} \gamma_2(v_i, v_j)\right]$  and  $\mu_2(v_i, v_j) = 0$ .

 $v_j$ ) =  $\gamma_2(v_i, v_j) = 0$  for  $v_i v_j \notin E$ . The **minimum degree** of G is  $\delta(G) = \min\{d_{\mu}(v_i), d_{\gamma}(v_i) | v_i \in V\}$ . The **maximum degree** of G is  $\Delta(G) = \max\{d_{\mu}(v_i), d_{\gamma}(v_i) | v_i \in V\}$ .

**Definition 2.8.** [8] The degree of a vertex v in an IFG G = (V, E) is defined to be sum of the weights of the strong edges incident at v. It is denoted by W(G).

**Definition 2.9.** [11] A subset D of V is called a **dominating set in an IFG** G if for every  $v \in V-D$ , there exists  $u \in D$  such that  $u, v \in E(G)$ .

**Definition 2.10.** [11] A dominating set D of an IFG is said to be **minimal dominating** set if no proper subset of D is a dominating set.

**Definition 2.11.** [7] A strong (weak) dominating set  $T_{\mu}$  of an intuitionistic fuzzy graph is said to be **semi-\mu strong (weak) dominating set** if  $\mu_2(v_i, v_j) = \min(\mu_1(v_i), \mu_1(v_j))$  for every  $v_i$  and  $v_j$ .

**Definition 2.12.** [5] Let G be an intuitionistic fuzzy Graph. A semi -  $\mu$  strong (weak) dominating set  $T_{\mu}$  of an IFG is said to be **total semi - \mu strong (weak) dominating set of intuitionistic fuzzy graph G** if  $d_N(u) \ge d_N(v)$  for all  $u \in T_{\mu}$ ,  $v \in V$ .

**Definition 2.13. [5]** A total semi -  $\mu$  strong (weak) dominating set  $T_{\mu}$  of an intuitionistic fuzzy graph G is called **minimal total semi - \mu strong (weak) dominating set** of G if  $v \in T_{\mu}$ ,  $T_{\mu}$  - {v} is not a total semi -  $\mu$  strong (weak) dominating set of G.

**Definition 2.14.** [5] The minimum fuzzy cardinality among all minimum total semi -  $\mu$  strong (weak) intuitionistic fuzzy dominating set in G is called **total semi - \mu strong** (weak) dominating number of G is denoted by  $\gamma_{T_{u}}(G)$ .

**Definition 2.15.** The **degree of effective edge** of  $e_i$  is the sum of the membership value of the effective edge incident on  $e_i$ , denoted by  $d_E(e_i)$ .

**Definition 2.16.** Let G be an intuitionistic fuzzy graph. The edge set  $T_e$  is said to be a **total edge dominating set** if for every edge in G dominates atleast one edge of  $T_e$ .

**Definition 2.17.** Let G be an intuitionistic fuzzy graph. The edge set T<sub>e</sub> is said to be **total** strong (weak) edge dominating set of G if

- i  $d_N(e_i) \ge d_N(e_j)$  for all  $e_i \in T_e, e_j \in E$
- ii  $T_{e}$  is a total edge dominating set.

**Definition 2.18.** A total strong (weak) dominating set  $T_e$  of an intuitionistic fuzzy graph G is called **minimal total strong (weak) edge dominating set** of G if  $v \in T_e$ ,  $T_{e^-} \{v\}$  is not total strong (weak) edge dominating set of G.

**Theorem 2.19.** In an IFG,  $W_{T_e}(G) \leq O_{T_e}(G) \leq S_{T_e}(G)$ 

**Proof:** Let G be an intuitionistic fuzzy graph. Sum of fuzzy vertex cardinality of an intuitionistic fuzzy graph but need not be a minimum of weighted total strong (weak) edge domination IFG of G. Therefore,  $W_{Te}(G) \leq O_{Te}(G)$ .  $S_{Te}(G)$  be a size of total strong (weak) edge dominating set but need not be a minimum of sum of fuzzy vertex cardinality of total strong (weak) edge dominating set, then  $O_{Te}(G) \leq S_{Te}(G)$ .

Hence,  $W_{T_e}(G) \leq O_{T_e}(G) \leq S_{T_e}(G)$ .

**Theorem 2.20.** In an IFG,  $W_{T_e}(G) \leq \delta_{T_e}(G) \leq \Delta_{T_e}(G)$ 

**Proof:** Let G be an intuitionistic fuzzy graph.  $\delta_{T_e}(G)$  is a minimum degree of total strong (weak) edge domination of IFG but need not be a minimum of weighted total strong (weak) edge domination in IFG, then  $W_{T_e}(G) \leq \delta_{T_e}(G)$ .  $\Delta_{T_e}(G)$  is a maximum degree of total strong (weak) edge domination of IFG but need not minimum of minimum degree of total strong (weak) edge domination of IFG. Therefore,  $\delta_{T_e}(G) \leq \Delta_{T_e}(G)$ .

Hence,  $W_{Te}(G) \le \delta_{Te}(G) \le \Delta_{Te}(G)$ .

#### 3. Main results

# Regular total semi - µ strong (weak) edge dominating set of an IFG

In this section, Regular total semi -  $\mu$  strong (weak) edge dominating number of an intuitionistic fuzzy graph is introduced and its parametric conditions are established. Let us consider  $p \le q$  throughout the paper.

**Definition 3.1.** A total semi -  $\mu$  strong (weak) edge dominating set  $eRT_{\mu}$  of a graph G is a **regular total semi - \mu strong (weak) edge dominating set** if all the edges have same degree.

**Definition 3.2.** A regular total semi -  $\mu$  strong (weak) edge dominating set  $eRT_{\mu}$  of a intuitionistic fuzzy graph G is called **minimal regular total semi - \mu strong (weak) edge dominating set** of G, if  $v \in eRT_{\mu}$ ,  $eRT_{\mu} - \{v\}$  is not a regular total semi -  $\mu$  strong (weak) edge dominating set of G.

**Definition 3.3.** The minimum fuzzy cardinality among all minimal regular total semi -  $\mu$  strong (weak) edge dominating set is called **regular total semi - \mu strong (weak) edge dominating set** and its regular total semi -  $\mu$  strong (weak) edge domination number is denoted by  $\gamma_{eRT_{\mu}}(G)$ .

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**Theorem 3.4.** In an IFG,  $\gamma_{eRT_u}(G) \le p \le q$ 

**Proof:** Let G be an IFG.  $\gamma_{eRT_{\mu}}$  be a regular total semi -  $\mu$  strong (weak) edge domination number of an IFG. p be a sum of fuzzy vertex cardinality of an IFG G but need be a minimum of a regular total semi -  $\mu$  strong (weak) edge domination number of an IFG.  $\gamma_{eRT_{\mu}}$  be a regular total semi -  $\mu$  strong (weak) edge domination number of an IFG is less than or equal to sum of fuzzy vertex cardinality of an IFG. That is,  $\gamma_{eRT_{\mu}}(G) \leq p$ . q

be a sum of fuzzy edge cardinality of a regular total semi -  $\mu$  strong (weak) edge domination of an IFG but need not be a minimum of sum of fuzzy vertex cardinality of a regular total semi -  $\mu$  strong (weak) edge domination of an IFG of G. Then, sum of fuzzy vertex cardinality is less than or equal to sum of edge cardinality of a regular total semi - $\mu$  strong (weak) edge domination of an IFG G. That is,  $p \leq q$ .

Hence,  $\gamma_{eRT_u}(G) \le p \le q$ .

**Theorem 3.5.** In an IFG of G,  $W_{eRT_{\mu}}(G) \leq O_{eRT_{\mu}}(G) \leq S_{eRT_{\mu}}(G)$ 

**Proof:** Let G be an IFG.  $\gamma_{eRT_{\mu}}$  be a regular total semi -  $\mu$  strong (weak) edge domination number of an IFG.

 $O_{eRT_{\mu}}(G)$  be an order of a regular total semi -  $\mu$  strong (weak) edge domination of an IFG of G but need not be a minimum of a weighted regular total semi -  $\mu$  strong (weak) edge domination of an IFG. Then, weighted regular total semi -  $\mu$  strong (weak) edge domination of an IFG of G is less than or equal to order of an IFG. That is,  $W_{eRT_{\mu}}(G) \leq O_{eRT_{\mu}}(G)$ .  $S_{eRT_{\mu}}(G)$  be a size of a regular total semi -  $\mu$  strong (weak) edge domination of an IFG but need not be a minimum of an order of an edge IFG of G. Then, an order of a regular total semi -  $\mu$  strong (weak) edge domination of an IFG is less than or equal to size of an edge IFG. That is,  $O_{eRT_{\mu}}(G) \leq S_{eRT_{\mu}}(G)$ .

Hence,  $W_{eRT_{\mu}}(G) \leq O_{eRT_{\mu}}(G) \leq S_{eRT_{\mu}}(G)$ 

**Theorem 3.6.** For an IFG,  $\gamma_{eRT_{\mu}}(G) \ge \left|\frac{p-q}{2}\right|$ 

**Proof:** Let G be an IFG.  $\gamma_{eRT_{\mu}}$  be a regular total semi -  $\mu$  strong (weak) edge domination number of an IFG. Let p be a sum of fuzzy vertex cardinality of an IFG G. Let q be a sum of fuzzy edge cardinality of an IFG G.

 $\left|\frac{p-q}{2}\right|$  be a fuzzy vertices but need not be a maximum of a regular total semi -  $\mu$ 

strong (weak) edge domination number of an IFG of G. Then, a regular total semi -  $\boldsymbol{\mu}$ 

strong (weak) edge domination number of an IFG of G is greater than or equal to  $\left|\frac{p}{q}\right|$ 

fuzzy vertices. Hence,  $\gamma_{eRT_{\mu}}(G) \ge \left|\frac{p-q}{2}\right|$ 

**Example 3.7.** Let G be an intuitionistic fuzzy graph. Let  $\gamma_{eR_T}$  be a regular total strong (weak) edge domination number of G.

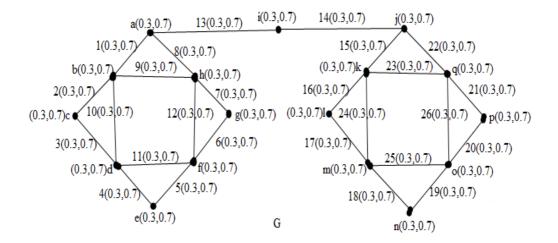


Figure 1:

$$\begin{split} R_{\text{Te}} &= \{1,3,5,7,15,17,19,21\}, E-R_{\text{Te}} = \{2,4,6,8,9,10,11,12,13,14,16,18,20,22\}, \\ p &= 4.2, \ q = 5.2, \ \gamma_{eR_{\text{T}}}(G) = 1.8 \ \Delta_{eN}(G) = 1.8, \ \delta_{eN}(G) = 1.6, \ |p-q| = |-1| = 1, \\ p - \Delta_{eN}(G) = 2.4, \ p - \delta_{eN}(G) = 2.6, \ q - \Delta_{eN}(G) = 3.4, \ q - \delta_{eN}(G) = 3.6. \end{split}$$

## 4. Equitable regular total semi - $\mu$ strong (weak) edge domination in an IFG

In this section, Equitable regular total semi -  $\mu$  strong (weak) edge dominating number of an intuitionistic fuzzy graph is introduced and its parametric conditions are established. Let us consider  $p \le q$  throughout the paper.

**Definition 4.1.** A regular total semi -  $\mu$  strong (weak) edge dominating set  $eERT_{\mu}$  of an intuitionistic fuzzy graph G is an **equitable regular total semi - \mu strong (weak) edge dominating set** if

i.  $u,v \in E(G)$  and

ii.  $|\deg(u) - \deg(v)| \le 1$  for all  $u \in ERT_{\mu}$ ,  $v \in V$ -ERT<sub> $\mu$ </sub>

**Definition 4.2.** An equitable regular total semi -  $\mu$  strong (weak) edge dominating set  $eERT_{\mu}$  of a intuitionistic fuzzy graph G is called **minimal equitable regular total semi -**

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 $\mu$  strong (weak) edge dominating set of G, if  $v \in eERT_{\mu}$ ,  $eERT_{\mu} - \{v\}$  is not an equitable regular total semi -  $\mu$  strong (weak) edge dominating set of G.

**Definition 4.3.** The minimum fuzzy cardinality among all minimal equitable regular total semi -  $\mu$  strong (weak) edge dominating set is called **equitable regular total semi - \mu** strong (weak) edge dominating set and its equitable regular total semi -  $\mu$  strong (weak) edge domination number is denoted by  $\gamma_{eERT_{\mu}}$  (G).

**Theorem 4.4.** For an intuitionistic fuzzy graph,  $\gamma_{eERT_{\mu}}(G) \leq p - \Delta_{e(\mu)}(G) \leq q - \delta_{e(\mu)}(G)$ 

**Proof:** Let G be an intuitionistic fuzzy graph. Let  $\gamma_{eERT_{\mu}}(G)$  be an equitable regular total semi -  $\mu$  strong (weak) edge domination number of G.

p -  $\Delta_{e(\mu)}$  be a fuzzy vertices but need not be a minimum of an equitable regular total semi -  $\mu$  strong (weak) edge domination number of G. Then, an equitable regular total semi -  $\mu$  strong (weak) edge domination number of G is less than or equal to p -  $\Delta_{e(\mu)}$ . That is,  $\gamma_{eERT_{\mu}}(G) \leq p - \Delta_{e(\mu)}(G)$ . q- $\delta_{e(\mu)}$  be a fuzzy vertices but need not be a minimum of p- $\Delta_{e(\mu)}$  fuzzy vertices. p-  $\Delta_{e(\mu)}$  fuzzy vertices is less than or equal to q- $\delta_{e(\mu)}$ .

$$\begin{split} \text{Therefore, } p &- \Delta_{e(\mu)}\left(G\right) \leq q - \delta_{e(\mu)}\left(G\right).\\ \text{Hence, } \gamma_{eRT_{\mu}}\left(G\right) \leq p - \Delta_{e(\mu)}\left(G\right) \leq p - \delta_{e(\mu)}\left(G\right). \end{split}$$

**Theorem 4.5.** For an intuitionistic fuzzy graph,  $\gamma_{eERT_{\mu}}(G) \le p - \Delta_{e(\gamma)}(G) \le q - \delta_{e(\gamma)}(G)$ 

**Proof:** Let G be an intuitionistic fuzzy graph. Let  $\gamma_{eRT_{\mu}}(G)$  be a regular total strong (weak) edge domination number of G.

 $\begin{array}{l} q \ - \ \Delta_{_{e(\gamma)}} \text{be a fuzzy edges but need not be a minimum of regular total strong} \\ (\text{weak}) \ \text{edge domination number of } G. \\ \text{Then, a regular total strong (weak) edge domination number of } G \\ \text{is less than or equal to } q \ - \ \Delta_{_{e(\gamma)}}. \\ \text{That is,} \\ \gamma_{eRT_{\mu}}(G) \leq q \ - \ \Delta_{_{e(\gamma)}}(G) \ . \\ q \ - \ \delta_{_{e(\gamma)}} \text{be a fuzzy vertices but need not be a minimum of } \\ q \ - \ \Delta_{_{e(\gamma)}} \text{fuzzy vertices.} \\ q \ - \ \Delta_{_{e(\gamma)}} \text{fuzzy vertices.} \\ \text{s less than or equal to } q \ - \ \delta_{_{e(\gamma)}} \\ \text{Therefore,} \\ q \ - \ \Delta_{_{e(\gamma)}}(G) \leq q \ - \ \delta_{_{e(\gamma)}}(G) \ . \\ \end{array}$ 

Hence,  $\gamma_{eERT_{\mu}}(G) \le p - \Delta_{e(\gamma)}(G) \le q - \delta_{e(\gamma)}(G)$ .

**Theorem 4.6.** For an intuitionistic fuzzy graph,  $\gamma_{eERT_{\mu}}(G) \ge \frac{p - \Delta_{e(\gamma)}(G)}{\Delta_{e(\mu)}(G) + 1}$ 

**Proof:** Let G be an intuitionistic fuzzy graph. Let  $\gamma_{eERT_{\mu}}$  be an equitable regular total strong (weak) edge domination number of G.  $\frac{p - \Delta_{e(\gamma)}(G)}{\Delta_{e(\mu)}(G) + 1}$  be a fuzzy vertices but need not be a maximum of an equitable regular total strong (weak) edge domination number of G. Hence,  $\gamma_{eERT_{\mu}}(G) \ge \frac{p - \Delta_{e(\gamma)}(G)}{\Delta_{e(\mu)}(G) + 1}$ .

Theorem 4.7. Let G be an IFG. In an IFG,

 $\frac{O_{e(\mu)}(G) - \Delta_{e(\mu)}(G)}{2} \leq \gamma_{eERT_{\mu}}(G) \leq \frac{O_{e(\gamma)}(G) - \Delta_{e(\gamma)}(G)}{2}$ 

**Proof:** Let G be an IFG.  $\gamma_{eERT_{\mu}}(G)$  be an equitable regular total semi -  $\mu$  strong (weak) edge domination of an IFG.  $\gamma_{eERT_{\mu}}(G)$  be an equitable regular total semi -  $\mu$  strong (weak) edge domination of an IFG but need not be a minimum of a  $\frac{O_{e(\mu)}(G) - \Delta_{e(\mu)}(G)}{2}$ 

fuzzy cardinality of IFG.  $\frac{O_{e(\mu)}(G) - \Delta_{e(\mu)}(G)}{2}$  fuzzy cardinality is less than or equal to an equitable regular total semi -  $\mu$  strong (weak) edge domination of an IFG. That is,  $\frac{O_{e(\mu)}(G) - \Delta_{e(\mu)}(G)}{2} \leq \gamma_{eERT_{\mu}}(G). \quad \frac{O_{e(\gamma)}(G) - \Delta_{e(\gamma)}(G)}{2}$  be a fuzzy vertices but need not be a minimum of an equitable regular total semi -  $\mu$  strong (weak) edge domination of

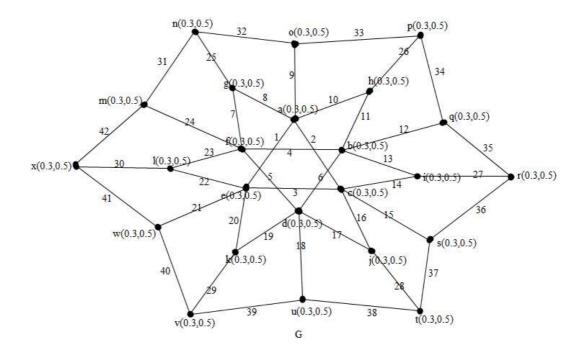
an IFG. Then, an equitable regular total semi -  $\mu$  strong (weak) edge domination of an  $O_{a(x)}(G) - \Delta_{a(x)}(G)$ 

IFG is less than or equal to a  $\frac{O_{e(\gamma)}(G) - \Delta_{e(\gamma)}(G)}{2}$  fuzzy vertices. That is,

$$\begin{split} \gamma_{eERT_{\mu}}(G) &\leq \frac{O_{e(\gamma)}(G) - \Delta_{e(\gamma)}(G)}{2}.\\ \text{Hence,} \ \frac{O_{e(\mu)}(G) - \Delta_{e(\mu)}(G)}{2} &\leq \gamma_{eERT_{\mu}}(G) \leq \frac{O_{e(\gamma)}(G) - \Delta_{e(\gamma)}(G)}{2}. \end{split}$$

**Example 4.8.** Let G be an IFG. All the edges have (0.3, 0.5) membership values. ERT<sub>µ</sub>={1,2,3,4,5,6,32,34,36,38,40,42},

 $\begin{aligned} & V - ERT_{\mu} = \\ & \{7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,23,24,25,26,27,28,29,30,31,33,35,37,39,41\}, \quad & \gamma_{eERT_{\mu}}(G) = 4.8, \ p = 9.6, \ q = 16.8, \ O(G) = (2.4,7.2), \ S(G) = (2.4,7.2), \ W(G) = \\ & (3.6,6), \ p - \Delta_{e(\gamma)}(G) = 8.1, \ q - \delta_{e(\gamma)}(G) = 15.3 \\ & p - \Delta_{e(\mu)}(G) = 8.7, \ p - \delta_{e(\mu)}(G) = 8.7, \ \Delta = \delta = (0.9,1.5) \end{aligned}$ 



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Figure 2:

# 5. Conclusion

In this paper, an equitable regular total semi -  $\mu$  strong (weak) edge domination number is defined and established the parametric conditions. The properties of Regular total semi -  $\mu$  strong (weak) edge domination number and an equitable regular total semi -  $\mu$  strong (weak) edge domination number are discussed.

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### REFERENCES

- 1. S.Arumugam and C.Natarajan, Strong (weak) domination in fuzzy graphs, *Intern. Journal of Computational and Mathematical Science*, 107(16) (2014) 16-18.
- 2. K.M.Dharmalingam and M.Rani, Equitable domination in fuzzy graphs, *Intern. Journal of Pure and Applied Mathematics*, 94(5) (2014) 661-667.
- 3. K.M.Dharmalingam and M.Rani, Total equitable domination in fuzzy graphs, Bulletin of the International Mathematical Virtual Institute, provide journal details
- 4. P.J. Jayalakshmi and C.V.R.Harinarayanan, Total strong (weak) domination in fuzzy graph, *Advances in Theoretical and Applied Mathematics*, 11(3) (2016) 203-212.
- 5. P.J. Jayalakshmi, C.V.R. Harinarayanan and R.Muthuraj, Total semi-µ strong (weak) Domination in IFG, *IOSR Journal of Mathematics*, 12(5) (2016) 37-43.

- V. R. Kulli and D.K. Patwari, On the total edge domination number of a graph, In A. M. Mathi, editor, *Proc. Of the Symp. On Graph Theory and Combinatorics*, Kochi, Centre Math. Sci., Trivandrum, 21 (1991) 75-81.
- 7. M.G. Karunambigai and R. Bhuvaneswari, Degrees in intuitionistic fuzzy graphs, *Annals of Fuzzy Mathematics and Informatics*, 10 (2016) 1 10.
- 8. A. NagoorGani and M. Basheer Ahamed, Order and size in fuzzy graph, *Bulletin of Pure and Applied Sciences*, 22 (2003) 145-148.
- 9. A. NagoorGani and K. Prasanna Devi, Edge domination and independence in fuzzy graphs, *Advances in Fuzzy Sets and Systems*, 15 (2013) 73-84.
- 10. A. NagoorGani and S. Shajitha Begum, Degree, order and size in intuitionistic fuzzy graphs, *International Journal of Algorithm, Computing and Mathematics*, 3 (2010) 11-16.
- 11. R. Parvathi and G. Tamizhendhi, Domination in intuitionistic fuzzy graphs, *NIFS* 16(2) (2010) 15-16.