

Multiplicative Connectivity KV Indices of Dendrimers

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Abstract. The connectivity indices are applied to measure the chemical characteristics of chemical compounds in chemistry. In this paper, we introduce the multiplicative sum connectivity KV index, multiplicative product connectivity KV index, multiplicative ABC KV index and multiplicative GA KV index of a molecular graph. We determine these multiplicative connectivity KV indices of POPAM dendrimers and tetrathiafulvalene dendrimers.

Keywords: multiplicative sum connectivity KV index, multiplicative product connectivity KV index, multiplicative ABC KV index, multiplicative GA KV index, dendrimers.

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1. Introduction

Let G be a finite, simple connected graph with vertex $V(G)$ and edge set $E(G)$. The degree $d(v)$ of a vertex v in G is the number of vertices adjacent to v . Let $M_G(v)$ denote the product of the degrees of all vertices adjacent to a vertex v . We refer to [1] for undefined term and notation.

Chemical Graph Theory is a branch of Mathematical Chemistry which has an important effect on the development of chemical sciences. Several topological indices have been considered in Theoretical Chemistry, especially in QSPR/QSAR research, see [1, 2].

Recently, Kulli introduced the first and second KV indices, defined as [4]

$$KV_1(G) = \sum_{uv \in E(G)} [M_G(u) + M_G(v)],$$

$$KV_2(G) = \sum_{uv \in E(G)} [M_G(u)M_G(v)].$$

Very recently, some novel variants of KV indices were studied such as hyper KV and square KV indices [5], connectivity KV indices [6], multiplicative KV indices and multiplicative hyper KV indices [7].

We introduce some multiplicative connectivity KV indices of a graph as follows:

The multiplicative sum connectivity KV index of a graph G is defined as

$$SKVII(G) = \prod_{uv \in E(G)} \frac{1}{\sqrt{M_G(u) + M_G(v)}} \quad (1)$$

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The multiplicative product connectivity *KV* index of a graph *G* is defined as

$$PKVII(G) = \prod_{uv \in E(G)} \frac{1}{\sqrt{M_G(u)M_G(v)}} \quad (2)$$

The multiplicative atom bond connectivity *KV* index of a graph *G* is defined as

$$ABCKVII(G) = \prod_{uv \in E(G)} \sqrt{\frac{M_G(u) + M_G(v) - 2}{M_G(u)M_G(v)}} \quad (3)$$

The multiplicative geometric-arithmetic *KV* index of a graph *G* is defined as

$$GAKVII(G) = \prod_{uv \in E(G)} \frac{2\sqrt{M_G(u)M_G(v)}}{M_G(u) + M_G(v)} \quad (4)$$

In recent years, some topological indices were studied, for example, in [8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19]. In this paper, some multiplicative connectivity *KV* indices for POPAM dendrimers and tetrathiafulvalene dendrimers are computed. For dendrimers, see [20].

2. Results for POPAM Dendrimers

The family of POPAM dendrimers is denoted by $POD_2[n]$. The graph of $POD_2[2]$ is shown in Figure 1.

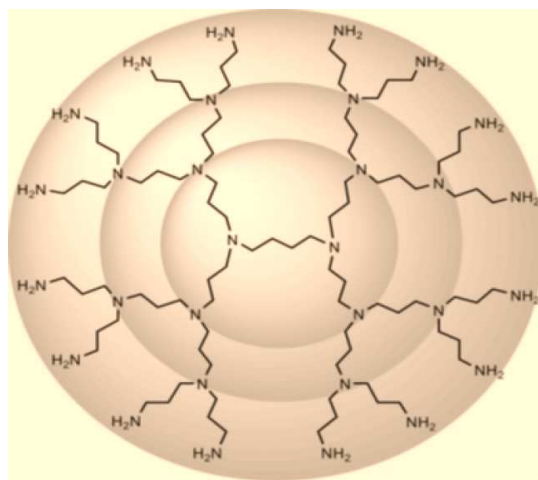


Figure 1: The graph of $POD_2[2]$

Let $G = POD_2[n]$. By algebraic method, we obtain that G has $2^{n+5} - 10$ vertices and $2^{n+5} - 11$ edges. The edge partition of $POD_2[n]$ based on the degree product of neighbors of end vertices of each edge is given in Table 1.

$M_G(u), M_G(v) \setminus uv \in E(G)$	(2, 2)	(2,4)	(4,4)	(4,6)	(6,8)
Number of edges	2^{n+2}	2^{n+2}	1	$3 \times 2^{n+2} - 6$	$3 \times 2^{n+2} - 6$

Table 1: Edge partition of $POD_2[n]$

Theorem 1. The multiplicative sum connectivity *KV* index of a POPAM dendrimer $POD_2[n]$ is

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$$SKVII(POD_2[n]) = \left(\frac{1}{2}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{6}}\right)^{2^{n+2}} \times \left(\frac{1}{2\sqrt{2}}\right)^1 \times \left(\frac{1}{\sqrt{10}}\right)^{3 \times 2^{n+2}-6} \times \left(\frac{1}{\sqrt{14}}\right)^{3 \times 2^{n+2}-6}$$

Proof: Let $G = POD_2[n]$. By using equation (1) and Table 1, we have

$$\begin{aligned} SKVII(POD_2[n]) &= \prod_{uv \in E(G)} \frac{1}{\sqrt{M_G(u) + M_G(v)}} \\ &= \left(\frac{1}{\sqrt{2+2}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{2+6}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{4+4}}\right)^1 \times \left(\frac{1}{\sqrt{4+6}}\right)^{3 \times 2^{n+2}-6} \times \left(\frac{1}{\sqrt{6+8}}\right)^{3 \times 2^{n+2}-6} \\ &= \left(\frac{1}{2}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{6}}\right)^{2^{n+2}} \times \left(\frac{1}{2\sqrt{2}}\right)^1 \times \left(\frac{1}{\sqrt{10}}\right)^{3 \times 2^{n+2}-6} \times \left(\frac{1}{\sqrt{14}}\right)^{3 \times 2^{n+2}-6} \end{aligned}$$

Theorem 2. The multiplicative product connectivity KV index of a POPAM dendrimer $POD_2[n]$ is

$$PKVII(POD_2[n]) = \left(\frac{1}{2}\right)^{2^{n+2}} \times \left(\frac{1}{2\sqrt{2}}\right)^{2^{n+2}} \times \frac{1}{4} \times \left(\frac{1}{2\sqrt{6}}\right)^{3 \times 2^{n+2}-6} \times \left(\frac{1}{4\sqrt{3}}\right)^{3 \times 2^{n+2}-6}$$

Proof: Let $G = POD_2[n]$. From equation (2), we have

$$PKVII(POD_2[n]) = \prod_{uv \in E(G)} \frac{1}{\sqrt{M_G(u)M_G(v)}}$$

By using Table 1, we deduce

$$\begin{aligned} PKVII(POD_2[n]) &= \left(\frac{1}{\sqrt{2 \times 2}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{2 \times 4}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{4 \times 4}}\right)^1 \times \left(\frac{1}{\sqrt{4 \times 6}}\right)^{3 \times 2^{n+2}-6} \times \left(\frac{1}{\sqrt{6 \times 8}}\right)^{3 \times 2^{n+2}-6} \\ &= \left(\frac{1}{2}\right)^{2^{n+2}} \times \left(\frac{1}{2\sqrt{2}}\right)^{2^{n+2}} \times \frac{1}{4} \times \left(\frac{1}{2\sqrt{6}}\right)^{3 \times 2^{n+2}-6} \times \left(\frac{1}{4\sqrt{3}}\right)^{3 \times 2^{n+2}-6} \end{aligned}$$

Theorem 3. The multiplicative atom bond connectivity KV index of a POPAM dendrimer $POD_2[n]$ is

$$ABCKVII(POD_2[n]) = \left(\frac{\sqrt{3}}{8}\right) \times \left(\frac{1}{2}\right)^{4 \times 2^{n+2}-6} \times \left(\frac{1}{\sqrt{3}}\right)^{3 \times 2^{n+2}-6}$$

Proof: Let $G = POD_2[n]$. By using equation (3) and Table 1, we derive

$$\begin{aligned} ABCKVII(POD_2[n]) &= \prod_{uv \in E(G)} \sqrt{\frac{M_G(u) + M_G(v) - 2}{M_G(u)M_G(v)}} \\ &= \left(\sqrt{\frac{2+2-2}{2 \times 2}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{2+4-2}{2 \times 4}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{4+4-2}{4 \times 4}}\right)^1 \times \left(\sqrt{\frac{4+6-2}{4 \times 6}}\right)^{3 \times 2^{n+2}-6} \times \left(\sqrt{\frac{6+8-2}{6 \times 8}}\right)^{3 \times 2^{n+2}-6} \\ &= \left(\frac{\sqrt{3}}{8}\right) \times \left(\frac{1}{2}\right)^{4 \times 2^{n+2}-6} \times \left(\frac{1}{\sqrt{3}}\right)^{3 \times 2^{n+2}-6} \end{aligned}$$

Theorem 4. The multiplicative geometric-arithmetic KV index of a POPAM dendrimer $POD_2[n]$

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$$GAKVII(POD_2[n]) = \left(\frac{2\sqrt{2}}{3}\right)^{2^{n+2}} \times \left(\frac{2\sqrt{6}}{5}\right)^{3 \times 2^{n+2} - 6} \times \left(\frac{4\sqrt{3}}{7}\right)^{3 \times 2^{n+2} - 6}.$$

Proof: Let $G = POD_2[n]$. By using equation (4), we obtain

$$GAKVII(POD_2[n]) = \prod_{uv \in E(G)} \frac{2\sqrt{M_G(u)M_G(v)}}{M_G(u) + M_G(v)}$$

Then by using Table 1, we deduce

$$\begin{aligned} GAKVII(POD_2[n]) &= \left(\frac{2\sqrt{2 \times 2}}{2+2}\right)^{2^{n+2}} \times \left(\frac{2\sqrt{2 \times 4}}{2+4}\right)^{2^{n+2}} \times \left(\frac{2\sqrt{4 \times 4}}{4+4}\right)^1 \times \left(\frac{2\sqrt{4 \times 6}}{4+6}\right)^{3 \times 2^{n+2} - 6} \times \left(\frac{2\sqrt{6 \times 8}}{6+8}\right)^{3 \times 2^{n+2} - 6} \\ &= \left(\frac{2\sqrt{2}}{3}\right)^{2^{n+2}} \times \left(\frac{2\sqrt{6}}{5}\right)^{3 \times 2^{n+2} - 6} \times \left(\frac{4\sqrt{3}}{7}\right)^{3 \times 2^{n+2} - 6}. \end{aligned}$$

3. Results for tetrathiafulvalene dendrimers

The family of tetrathiafulvalene dendrimers is denoted by $TD_2[n]$, where n is the steps of growth in this type of dendrimers, see Figure 2.

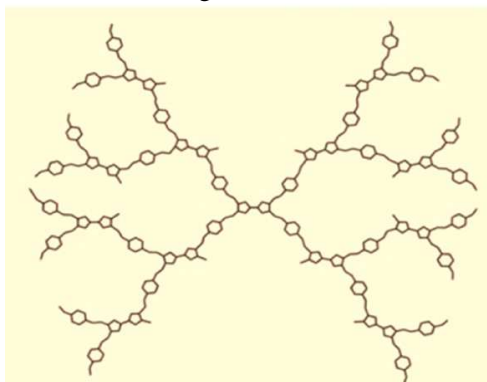


Figure 2: The graph of $TD_2[2]$

Let $G = TD_2[n]$. By algebraic method, we obtain that G has $31 \times 2^{n+2} - 24$ vertices and $32 \times 2^{n+2} - 85$ edges. The edge partition of G based on the degree product of neighbors of end vertices of each edge is given in Table 2.

$M_G(u), M_G(v) \setminus uv \in E(G)$	Number of edges
(2, 3)	2^{n+2}
(3, 6)	$2^{n+2} - 4$
(3, 8)	2^{n+2}
(6, 6)	$7 \times 2^{n+2} - 16$
(6, 8)	$11 \times 2^{n+2} - 24$
(6, 9)	$2^{n+2} - 4$
(6, 12)	$3 \times 2^{n+2} - 8$
(9, 12)	$8 \times 2^{n+2} - 24$
(12, 12)	$2 \times 2^{n+2} - 5$

Table 2: Edge partition of $TD_2[n]$

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Theorem 5. The multiplicative sum connectivity KV index of a tetrathiafulvalene dendrimer $TD_2[n]$ is

$$SKVII(TD_2[n]) = \left(\frac{1}{\sqrt{5}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{3}}\right)^{2^{n+2}-4} \times \left(\frac{1}{\sqrt{11}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{12}}\right)^{7 \times 2^{n+2}-6} \times \left(\frac{1}{\sqrt{14}}\right)^{11 \times 2^{n+2}-24} \\ \times \left(\frac{1}{\sqrt{15}}\right)^{2^{n+2}-4} \times \left(\frac{1}{\sqrt{18}}\right)^{3 \times 2^{n+2}-8} \times \left(\frac{1}{\sqrt{21}}\right)^{8 \times 2^{n+2}-24} \times \left(\frac{1}{\sqrt{24}}\right)^{2 \times 2^{n+2}-5}$$

Proof: Let $G = TD_2[n]$. From equation (1) and using Table 2, we derive

$$SKVII(TD_2[n]) = \prod_{uv \in E(G)} \frac{1}{\sqrt{M_G(u) + M_G(v)}} \\ = \left(\frac{1}{\sqrt{2+3}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{3+6}}\right)^{2^{n+2}-4} \times \left(\frac{1}{\sqrt{3+8}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{6+6}}\right)^{7 \times 2^{n+2}-6} \times \left(\frac{1}{\sqrt{6+8}}\right)^{11 \times 2^{n+2}-24} \\ \times \left(\frac{1}{\sqrt{6+9}}\right)^{2^{n+2}-4} \times \left(\frac{1}{\sqrt{6+12}}\right)^{3 \times 2^{n+2}-8} \times \left(\frac{1}{\sqrt{9+12}}\right)^{8 \times 2^{n+2}-24} \times \left(\frac{1}{\sqrt{12+12}}\right)^{2 \times 2^{n+2}-5} \\ = \left(\frac{1}{\sqrt{5}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{3}}\right)^{2^{n+2}-4} \times \left(\frac{1}{\sqrt{11}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{12}}\right)^{7 \times 2^{n+2}-6} \times \left(\frac{1}{\sqrt{14}}\right)^{11 \times 2^{n+2}-24} \\ \times \left(\frac{1}{\sqrt{15}}\right)^{2^{n+2}-4} \times \left(\frac{1}{\sqrt{18}}\right)^{3 \times 2^{n+2}-8} \times \left(\frac{1}{\sqrt{21}}\right)^{8 \times 2^{n+2}-24} \times \left(\frac{1}{\sqrt{24}}\right)^{2 \times 2^{n+2}-5}$$

Theorem 6. The multiplicative product connectivity KV index of $TD_2[n]$ is

$$PKVII(TD_2[n]) = \left(\frac{1}{\sqrt{6}}\right)^{2^{n+2}} \times \left(\frac{1}{3\sqrt{2}}\right)^{2^{n+2}-4} \times \left(\frac{1}{2\sqrt{6}}\right)^{2^{n+2}} \times \left(\frac{1}{6}\right)^{7 \times 2^{n+2}-16} \times \left(\frac{1}{4\sqrt{3}}\right)^{11 \times 2^{n+2}-24} \\ \times \left(\frac{1}{3\sqrt{6}}\right)^{2^{n+2}-4} \times \left(\frac{1}{6\sqrt{2}}\right)^{3 \times 2^{n+2}-8} \times \left(\frac{1}{6\sqrt{3}}\right)^{8 \times 2^{n+2}-24} \times \left(\frac{1}{12}\right)^{2 \times 2^{n+2}-5}$$

Proof: Let $G = TD_2[n]$. From equation (2) and by using Table 2, we obtain

$$PKVII(TD_2[n]) = \prod_{uv \in E(G)} \frac{1}{\sqrt{M_G(u)M_G(v)}} \\ = \left(\frac{1}{\sqrt{2 \times 3}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{3 \times 6}}\right)^{2^{n+2}-4} \times \left(\frac{1}{\sqrt{3 \times 8}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{6 \times 6}}\right)^{7 \times 2^{n+2}-16} \times \left(\frac{1}{\sqrt{6 \times 8}}\right)^{11 \times 2^{n+2}-24} \\ \times \left(\frac{1}{\sqrt{6 \times 9}}\right)^{2^{n+2}-4} \times \left(\frac{1}{\sqrt{6 \times 12}}\right)^{3 \times 2^{n+2}-8} \times \left(\frac{1}{\sqrt{9 \times 12}}\right)^{8 \times 2^{n+2}-24} \times \left(\frac{1}{\sqrt{12 \times 12}}\right)^{2 \times 2^{n+2}-5} \\ = \left(\frac{1}{\sqrt{6}}\right)^{2^{n+2}} \times \left(\frac{1}{3\sqrt{2}}\right)^{2^{n+2}-4} \times \left(\frac{1}{2\sqrt{6}}\right)^{2^{n+2}} \times \left(\frac{1}{6}\right)^{7 \times 2^{n+2}-16} \times \left(\frac{1}{4\sqrt{3}}\right)^{11 \times 2^{n+2}-24} \\ \times \left(\frac{1}{3\sqrt{6}}\right)^{2^{n+2}-4} \times \left(\frac{1}{6\sqrt{2}}\right)^{3 \times 2^{n+2}-8} \times \left(\frac{1}{6\sqrt{3}}\right)^{8 \times 2^{n+2}-24} \times \left(\frac{1}{12}\right)^{2 \times 2^{n+2}-5} .$$

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Theorem 7. The multiplicative atom bond connectivity KV index of $TD_2[n]$ is

$$ABCKVII(TD_2[n]) = \left(\frac{1}{\sqrt{2}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{7}{18}}\right)^{2^{n+2}-4} \times \left(\sqrt{\frac{3}{8}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{5}{18}}\right)^{7 \times 2^{n+2}-16} \\ \times \left(\frac{1}{2}\right)^{11 \times 2^{n+2}-24} \times \left(\sqrt{\frac{13}{54}}\right)^{2^{n+2}-4} \times \left(\sqrt{\frac{2}{9}}\right)^{3 \times 2^{n+2}-8} \times \left(\sqrt{\frac{19}{108}}\right)^{8 \times 2^{n+2}-24} \times \left(\sqrt{\frac{11}{72}}\right)^{2 \times 2^{n+2}-5}$$

Proof: Let $G = TD_2[n]$. By using equation (3) and Table 2, we deduce

$$ABCKVII(TD_2[n]) = \prod_{uv \in E(G)} \sqrt{\frac{M_G(u) + M_G(v) - 2}{M_G(u)M_G(v)}} \\ = \left(\sqrt{\frac{2+3-2}{2 \times 3}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{3+6-2}{3 \times 6}}\right)^{2^{n+2}-4} \times \left(\sqrt{\frac{3+8-2}{3 \times 8}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{6+6-2}{6 \times 6}}\right)^{7 \times 2^{n+2}-16} \\ \times \left(\sqrt{\frac{6+8-2}{6 \times 8}}\right)^{11 \times 2^{n+2}-24} \times \left(\sqrt{\frac{6+9-2}{6 \times 9}}\right)^{2^{n+2}-4} \times \left(\sqrt{\frac{6+12-2}{6 \times 12}}\right)^{3 \times 2^{n+2}-8} \\ \times \left(\sqrt{\frac{9+12-2}{9 \times 12}}\right)^{8 \times 2^{n+2}-24} \times \left(\sqrt{\frac{12+12-2}{12 \times 12}}\right)^{2 \times 2^{n+2}-5} \\ = \left(\frac{1}{\sqrt{2}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{7}{18}}\right)^{2^{n+2}-4} \times \left(\sqrt{\frac{3}{8}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{5}{18}}\right)^{7 \times 2^{n+2}-16} \times \left(\frac{1}{2}\right)^{11 \times 2^{n+2}-24} \\ \times \left(\sqrt{\frac{13}{54}}\right)^{2^{n+2}-4} \times \left(\sqrt{\frac{2}{9}}\right)^{3 \times 2^{n+2}-8} \times \left(\sqrt{\frac{19}{108}}\right)^{8 \times 2^{n+2}-24} \times \left(\sqrt{\frac{11}{72}}\right)^{2 \times 2^{n+2}-5}$$

Theorem 8. The multiplicative geometric-arithmetic KV index of $TD_2[n]$ is

$$GAKVII(TD_2[n]) = \left(\frac{2\sqrt{6}}{5}\right)^{2 \times 2^{n+2}-4} \times \left(\frac{2\sqrt{2}}{3}\right)^{4 \times 2^{n+2}-12} \times \left(\frac{4\sqrt{6}}{11}\right)^{2^{n+2}} \times \left(\frac{4\sqrt{3}}{7}\right)^{19 \times 2^{n+2}-48}$$

Proof: Let $G = TD_2[n]$. By using equation (4) and Table 2, we obtain

$$GAKVII(TD_2[n]) = \prod_{uv \in E(G)} \frac{2\sqrt{M_G(u)M_G(v)}}{M_G(u) + M_G(v)} \\ = \left(\frac{2\sqrt{2 \times 3}}{2+3}\right)^{2^{n+2}} \times \left(\frac{2\sqrt{3 \times 6}}{3+6}\right)^{2^{n+2}-4} \times \left(\frac{2\sqrt{3 \times 8}}{3+8}\right)^{2^{n+2}} \times \left(\frac{2\sqrt{6 \times 6}}{6+6}\right)^{7 \times 2^{n+2}-16} \times \left(\frac{2\sqrt{6 \times 8}}{6+8}\right)^{11 \times 2^{n+2}-24} \\ \times \left(\frac{2\sqrt{6 \times 9}}{6+9}\right)^{2^{n+2}-4} \times \left(\frac{2\sqrt{6 \times 12}}{6+12}\right)^{3 \times 2^{n+2}-8} \times \left(\frac{2\sqrt{9 \times 12}}{9+12}\right)^{8 \times 2^{n+2}-24} \times \left(\frac{2\sqrt{12 \times 12}}{12+12}\right)^{2 \times 2^{n+2}-5} \\ = \left(\frac{2\sqrt{2}}{5}\right)^{2 \times 2^{n+2}-4} \times \left(\frac{2\sqrt{6}}{3}\right)^{4 \times 2^{n+2}-12} \times \left(\frac{4\sqrt{6}}{11}\right)^{2^{n+2}} \times \left(\frac{4\sqrt{3}}{7}\right)^{19 \times 2^{n+2}-48}$$

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